

Consider the differential equation $\frac{dy}{dx} = \frac{y+1}{x^3}$.

Find the particular solution $y = f(x)$ to the differential equation with initial condition $y(1) = e^2$.