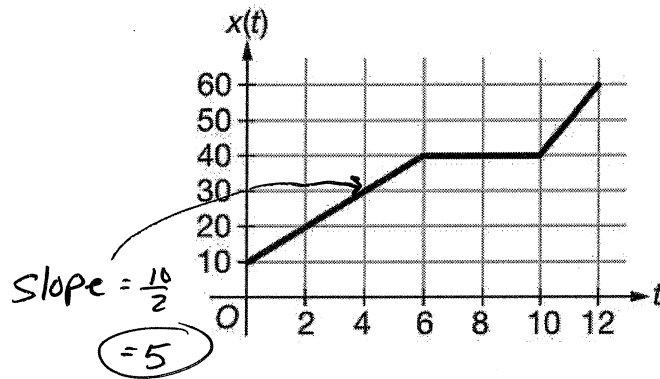


Unit 3 AP Classroom Practice for Sections 1-5

1)



A particle is moving on the x -axis and the position of the particle at time t is given by $x(t)$, whose graph is shown above. Which of the following is the best estimate for the speed of the particle at time $t = 4$?

- (A) 0
- (B) 5
- (C) $\frac{15}{2}$
- (D) 10

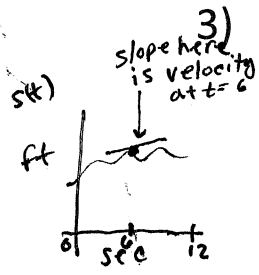
2)

x	-2	-1	0	1	2
$g(x)$	-3	2	1	0	5

$$\frac{g(2) - g(-2)}{2 - (-2)} = \frac{5 - (-3)}{4}$$

Selected values of a function g are shown in the table above. What is the average rate of change of g over the interval $[-2, 2]$?

- (A) $\frac{2 - (-2)}{5 - (-3)}$
- (B) $\frac{5 - (-3)}{2 - (-2)}$
- (C) $\frac{5 + (-3)}{2}$
- (D) $\frac{-3 + 2 + 1 + 0 + 5}{5}$



A car is driven on a straight road, and the distance traveled by the car after time $t = 0$ is given by a quadratic function s , where $s(t)$ is measured in feet and t is measured in seconds for $0 \leq t \leq 12$. Of the following, which gives the best estimate of the velocity of the car, in feet per second, at time $t = 6$ seconds?

(A) $s(6)$

(B) $\frac{s(6)}{6}$

(C) $\frac{s(8) - s(4)}{8 - 4}$

(D) $\frac{s(7) - s(5)}{7 - 5}$

Using average ROC to estimate instantaneous ROC

"6" is between 5 & 7

4) Let f be the function defined by $f(x) = e^{2x}$. The average rate of change of f over the interval $[1, b]$ is 20, where $b > 1$. Which of the following is an equation that could be used to find the value of b ?

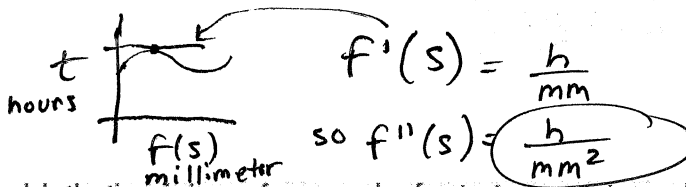
(A) $f(b) = 20$

(B) $f(b) - f(1) = 20$

(C) $\frac{f(b) - f(1)}{b - 1} = 20$

(D) $\frac{f(b) + f(1)}{2} = 20$

$$\frac{f(b) - f(1)}{b - 1} = 20$$



5) The function $t = f(S)$ models the time, in hours, for a sample of water to evaporate as a function of the size S of the sample, measured in milliliters. What are the units for $f''(S)$?

- (A) hours per milliliter
- (B) milliliters per hour
- (C) hours per milliliter per milliliter
- (D) milliliters per hour per hour

6) Graphing Calculator Needed

$$D(t) = 10 + 4.9 \cos\left(\frac{\pi}{6}t\right)$$

The function D defined above models the depth, in feet, of the water t hours after 12 A.M. in a certain harbor. Which of the following presents the method for finding the instantaneous rate of change of the depth of the water, in feet per hour, at 6 A.M.?

$D'(6)$

- (A) $\frac{D(6) - D(0)}{6 - 0} = -1.633$
- (B) $D'(6) = 0$
- (C) $D''(6) = 1.343$
- (D) $D(6) = 5.100$

$$v(t) = 1(a-t)' \cdot (-1)$$

$$-a + t > 0$$

$$t > a$$

- 7) A particle moves along the x -axis so that at any time $t \geq 0$ its position is given by $x(t) = \frac{1}{2}(a-t)^2$, where a is a positive constant. For what values of t is the particle moving to the right? $v(t) > 0$

(A) The particle is moving to the right only if $0 < t < a$.

(B) The particle is moving to the right only if $a < t$.

(C) The particle is moving to the right only if $t = a$.

(D) The particle is not moving to the right.

- 8) An object moves along a straight line so that at any time t , $0 \leq t \leq 9$, its position is given by $x(t) = 7 + 6t - t^2$. For what value of t is the object at rest? $v(t) = 0$

(A) $t = 3$

(B) $t = 6$

(C) $t = \frac{13}{2}$

(D) $t = 7$

$$v(t) = 0 + 6 - 2t$$

$$0 = 6 - 2t$$

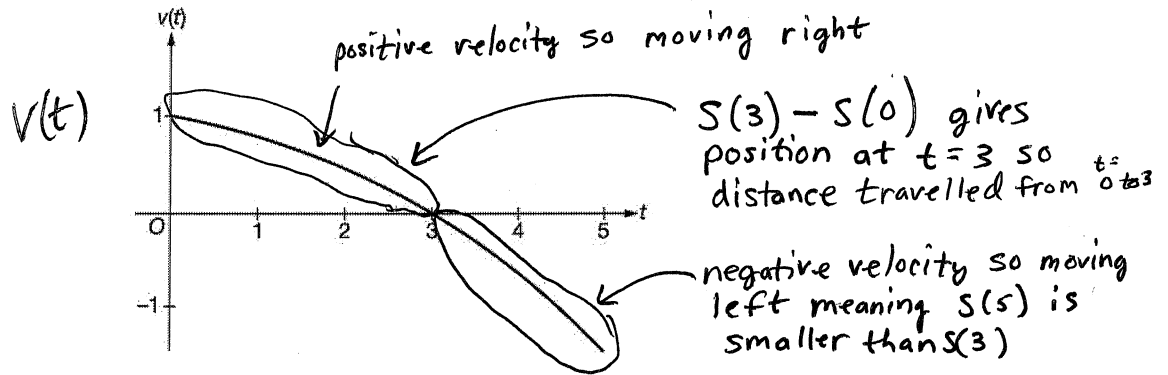
$$-6 = -2t$$

$$\frac{-6}{-2} = t$$

$$3 = t$$

9)

Tough!



A particle traveling on the x -axis has position $x(t)$ at time t . The graph of the particle's velocity $v(t)$ is shown above for $0 \leq t \leq 5$. Which of the following expressions gives the total distance traveled by the particle over the time interval $0 \leq t \leq 5$?

- (A) $x(0) - x(5)$
- (B) $x(5) - x(0)$
- (C) $(x(3) - x(0)) + (x(3) - x(5))$
- (D) $(x(0) - x(3)) + (x(5) - x(3))$

$S(3) - S(0)$ is distance from $t=0$ to $t=3$
 $S(3) - S(5)$ is distance from $t=3$ to $t=5$

10) Let x and y be functions of time t such that the sum of x and twice y is constant. Which of the following equations describes the relationship between the rate of change of x with respect to time and the rate of change of y with respect to time?

$$x + 2y = C$$

- (A) $\frac{dx}{dt} = 2 \frac{dy}{dt}$
- (B) $\frac{dx}{dt} = -2 \frac{dy}{dt}$
- (C) $2 \frac{dx}{dt} + \frac{dy}{dt} = 0$
- (D) $\frac{dx}{dt} + 2 \frac{dy}{dt} = K$, where K is a function of t

If

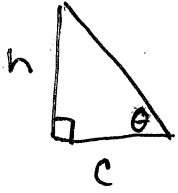
$$x + 2y = C$$

$$\frac{dx}{dt} + 2 \frac{dy}{dt} = 0$$

deriv. of constant is zero

$$\frac{dx}{dt} = -2 \frac{dy}{dt}$$

- 11) A right triangle has base x feet and height h feet, where x is constant and h changes with respect to time t , measured in seconds. The angle θ , measured in radians, is defined by $\tan \theta = \frac{h}{x}$. Which of the following best describes the relationship between $\frac{d\theta}{dt}$, the rate of change of θ with respect to time, and $\frac{dh}{dt}$, the rate of change of h with respect to time?



$$\tan \theta = \frac{h}{x}$$

$$\theta = \tan^{-1}\left(\frac{h}{x}\right)$$

$$\frac{d\theta}{dt} = \frac{1}{1+\left(\frac{h}{x}\right)^2} \cdot \frac{1}{x} \frac{dh}{dt}$$

$$\frac{d\theta}{dt} = \frac{1}{1+\frac{h^2}{x^2}} \cdot \frac{1}{x} \frac{dh}{dt}$$

$$\frac{d\theta}{dt} = \frac{1}{x+\frac{h^2}{x}} \frac{dh}{dt}$$

$$\frac{d\theta}{dt} = \frac{x}{x^2+h^2} \frac{dh}{dt}$$

(A) $\frac{d\theta}{dt} = \left(\frac{x}{x^2+h^2}\right) \frac{dh}{dt}$ radians per second

(B) $\frac{d\theta}{dt} = \left(\frac{x^2}{x^2+h^2}\right) \frac{dh}{dt}$ radians per second

(C) $\frac{d\theta}{dt} = \left(\frac{1}{\sqrt{x^2+h^2}}\right) \frac{dh}{dt}$ radians per second

(D) $\frac{d\theta}{dt} = \tan^{-1}\left(\frac{1}{x} \frac{dh}{dt}\right)$ radians per second

- 12) A particle moves on the hyperbola $xy = 15$ for time $t \geq 0$ seconds. At a certain instant, $x = 3$ and $\frac{dx}{dt} = 6$. Which of the following is true about y at this instant?

NOTE ALL ANSWERS are how "y" is changing
So find $\frac{dy}{dt}$

(A) y is decreasing by 10 units per second.

(B) y is increasing by 10 units per second.

(C) y is decreasing by 5 units per second.

(D) y is increasing by 5 units per second.

$$x \cdot \frac{dy}{dt} + y \frac{dx}{dt} = 0$$

$$\frac{dy}{dt} = \frac{-y \frac{dx}{dt}}{x}$$

$$\frac{dy}{dt} = \frac{-5 \cdot 6}{3} = \frac{-30}{3} = -10$$

decreasing

If $xy = 15$
when $x = 3 \dots y = 5$

$$\frac{dV}{dt} = \pi \left(r^2 \frac{dh}{dt} + 2rh \frac{dr}{dt} \right)$$

$$= \pi (2^2 \cdot (3) + 2 \cdot 2 \cdot 20 \cdot (-.1))$$

$\rightarrow = \pi (12 + (-8))$
 $= \pi \cdot 4$

- 13) A piece of rubber tubing maintains a cylindrical shape as it is stretched. At the instant that the inner radius of the tube is 2 millimeters and the height is 20 millimeters, the inner radius is decreasing at the rate of 0.1 millimeter per second and the height is increasing at the rate of 3 millimeters per second. Which of the following statements about the volume of the tube is true at this instant? (The volume V of a cylinder with radius r and height h is $V = \pi r^2 h$.)

NOTE! Answers are "how volume is changing" so find $\frac{dV}{dt}$

- (A) ^{$\frac{dV}{dt}$ is positive} The volume is increasing by 4π cubic millimeters per second.
- (B) The volume is decreasing by 4π cubic millimeters per second.
- (C) The volume is increasing by 20π cubic millimeters per second.
- (D) The volume is decreasing by 20π cubic millimeters per second.

- 14) how many times is the AVG ROC = 6

x	1	3	5	7	9
$f(x)$	0	6	18	29	42

on $[3, 5]$ AVG ROC = 6
 on $[5, 9]$ AVG ROC = 6

Selected values of a differentiable function f are given in the table above. What is the fewest possible number of values of c in the interval $[1, 9]$ for which the Mean Value Theorem guarantees that $f'(c) = 6$?

- (A) Zero
- (B) One
- (C) Two
- (D) Three

15) The Mean Value Theorem can be applied to which of the following functions on the closed interval $[-5, 5]$?
 Must be continuous & differentiable

(A) ~~$f(x) = \frac{1}{\sin x}$~~ asymptote at $x=0$

(B) ~~$f(x) = \frac{x-1}{|x-1|}$~~ jump at $x=1$

(C) $f(x) = \frac{x^2}{x^2-36}$ asymptotes at $x = \pm 6$ ← but not on the interval

(D) ~~$f(x) = \frac{x^2}{x^2-4}$~~ asymptotes at $x = \pm 2$

16) Which of the following functions of x is guaranteed by the Extreme Value Theorem to have an absolute maximum on the interval $[0, 2\pi]$? $f(a)$ & $f(b)$ exist and function must be continuous on $[0, 2\pi]$ so closed interval $[a, b]$

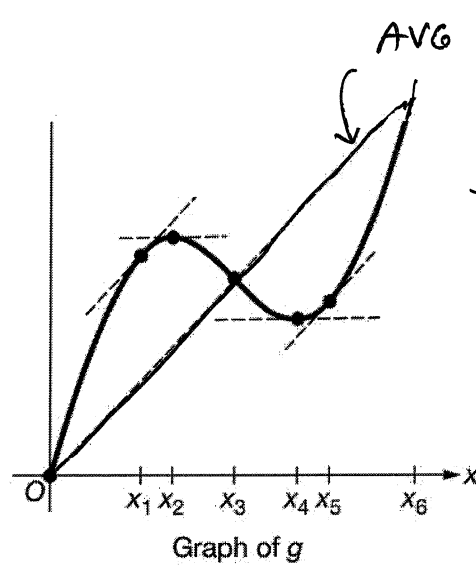
(A) $y = \frac{1}{1+\sin x}$ asymptote at $x = \frac{3\pi}{2}$

(B) $y = \frac{1}{x^2+\pi}$

(C) $y = \frac{(x-\pi)(x-\pi)}{x-\pi}$ hole at $x = \pi$

(D) $y = \frac{|x-\pi|}{x-\pi}$ jump at $x = \pi$

17)



The function g shown in the figure above is continuous on the closed interval $[0, x_6]$ and differentiable on the open interval $(0, x_6)$, where x_1, x_2, x_3, x_4, x_5 , and x_6 are points on the x -axis. Based on the graph, what are all values of x that satisfy the conclusion of the Mean Value Theorem applied to g on the closed interval $[0, x_6]$?

- (A) x_3 only, because this is the value where $g(x)$ equals the average rate of change of g on $[0, x_6]$.
- (B) x_2 and x_4 only, because these are the values where $g'(x) = 0$ on $[0, x_6]$.
- (C) x_1 and x_5 only, because these are the values where the instantaneous rate of change of g at those values is equal to the average rate of change of g on $[0, x_6]$.
- (D) x_1, x_3 , and x_5 only, because these are the values where either the instantaneous rate of change of g at the value is equal to the average rate of change of g on $[0, x_6]$ or the value of $g(x)$ is equal to the average rate of change of g on $[0, x_6]$.

18)

x	0	1	2	3
$f(x)$	0	4	7	6

Let f be a function with selected values given in the table above. Which of the following statements must be true? Assuming $f(x)$ is continuous & differentiable

All true if continuous & differentiable

- I. By the Intermediate Value Theorem, there is a value c in the interval $(0, 3)$ such that $f(c) = 2$.
- II. By the Mean Value Theorem, there is a value c in the interval $(0, 3)$ such that $f'(c) = 2$.
- III. By the Extreme Value Theorem, there is a value c in the interval $[0, 3]$ such that $f(c) \leq f(x)$ for all x in the interval $[0, 3]$.

Yes $f(0) = 0$
 $f(3) = 6$
 \uparrow
 all values between 0 & 6 will occur

- (A) None
- (B) I only
- (C) II only
- (D) I, II, and III

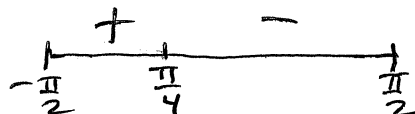
19) Let f be the function defined by $f(x) = (\sin x)e^{-x}$ on the interval $[-\frac{\pi}{2}, \frac{\pi}{2}]$. On which of the following open intervals is f increasing?

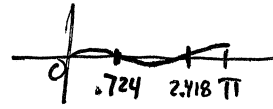
$$f'(x) = \sin x \cdot (-e^{-x}) + e^{-x} \cdot \cos x$$

$$= e^{-x} \cdot (-\sin x + \cos x)$$

$e^{-x} > 0$
 $-\sin x + \cos x = 0$
 $1 = \tan x$
 $x = \frac{\pi}{4}$

- (A) $(-\frac{\pi}{4}, \frac{\pi}{2})$
- (B) $(0, \frac{\pi}{2})$ only
- (C) $(\frac{\pi}{4}, \frac{\pi}{2})$ only
- (D) $(-\frac{\pi}{2}, \frac{\pi}{4})$





20) Graphing Calculator Needed

Let f be the function with derivative given by $f'(x) = \sin x + \cos(2x) - \frac{\pi}{4}$ for $0 \leq x \leq \pi$. On which of the following intervals is f increasing?

whenever $f'(x) > 0$ (above the x -axis)

(A) $[0, 0.724]$ only

(B) $[0, 0.724]$ and $[2.418, 3.142]$

(C) $[0, 0.253]$ and $[1.571, 2.889]$

(D) $[0.724, 2.418]$

21) Let f be the function with derivative given by $f'(x) = x^2 - a^2 = (x - a)(x + a)$, where a is a positive constant. Which of the following statements is true?

(A) f is decreasing for $-a < x < a$ because $f'(x) < 0$ for $-a < x < a$.

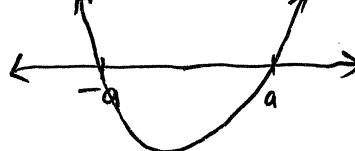
(B) f is decreasing for $x < -a$ and $x > a$ because $f'(x) < 0$ for $x < -a$ and $x > a$.

(C) f is decreasing for $x < 0$ because $f'(x) < 0$ for $x < 0$.

(D) f is decreasing for $x < 0$ because $f''(x) < 0$ for $x < 0$.

$f'(x) = x^2 - a^2$
 \uparrow
 a parabola opening upward

$$f'(x) = (x-a)(x+a)$$



f inc $(-\infty, -a) \cup (a, \infty)$
 f dec $(-a, a)$

$$0 = (x-a)(x+a)$$

$$x = a \text{ or } x = -a$$

$$f'(x) = x^2 \cdot e^{-x^2} \cdot (-2x) + e^{-x^2} \cdot 2x$$

$$f'(x) = x e^{-x^2} \cdot (-2x^2 + 2)$$

22) The function f is defined by $f(x) = x^2 e^{-x^2}$. At what values of x does f have a relative maximum?

(A) -2

(B) 0

(C) 1 only

(D) -1 and 1

$$0 = x \cdot e^{-x^2} \cdot (-2x^2 + 2)$$

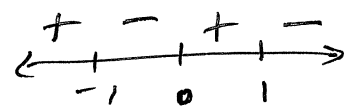
$x=0$

$e^{-x^2} \neq 0$

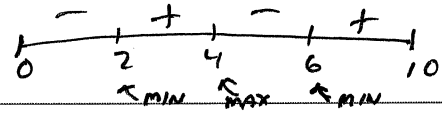
$-2x^2 + 2 = 0$

$x^2 = 1$

$x = \pm 1$



23) Let f be a differentiable function with a domain of $(0, 10)$. It is known that $f'(x)$, the derivative of $f(x)$, is negative on the intervals $(0, 2)$ and $(4, 6)$ and positive on the intervals $(2, 4)$ and $(6, 10)$. Which of the following statements is true?



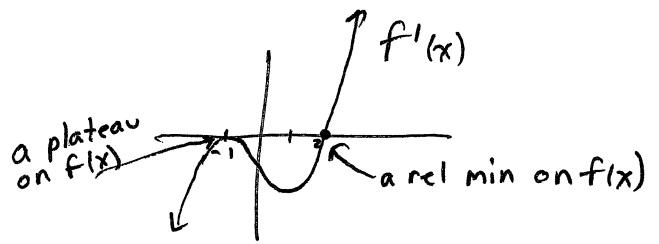
(A) f has no relative minima and three relative maxima.

(B) f has one relative minimum and two relative maxima.

(C) f has two relative minima and one relative maximum.

(D) f has three relative minima and no relative maxima.

24) Graphing Calculator Needed



Let f be the function with derivative $f'(x) = x^3 - 3x - 2$. Which of the following statements is true?

(A) f has no relative minima and one relative maximum.

(B) f has one relative minimum and no relative maxima.

(C) f has one relative minimum and one relative maximum.

(D) f has two relative minima and one relative maximum.

25) Let g be the function defined by $g(x) = |x| - 3|x + 1|$. What is the absolute maximum value of g on the closed interval $[-2, 2]$?

will have sharp turns at $x=0$ & $x=-1$

(A) 1

(B) -1

(C) -3

(D) -7

$$\begin{aligned} g(0) &= |0| - 3|0+1| \\ &= 0 - 3 \cdot 1 \\ &= 0 - 3 \\ &= -3 \end{aligned}$$

$$\begin{aligned} g(-1) &= |-1| - 3|-1+1| \\ &= 1 - 3 \cdot 0 \\ &= 1 \end{aligned}$$

$$g(x) = |x| - 3|x+1|$$

$$\begin{aligned} g(-2) &= |-2| - 3|-2+1| \\ &= 2 - 3 \cdot 1 \\ &= -1 \end{aligned}$$

$$\begin{aligned} g(2) &= |2| - 3|2+1| \\ &= 2 - 3 \cdot 3 \\ &= 2 - 9 \\ &= -7 \end{aligned}$$

$$f'(x) = 6x - 3x^2$$

$$0 = 3x(2-x)$$

$$3x = 0$$

$$x = 0$$

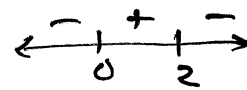
$$2-x = 0$$

$$x = 2$$

26) Let f be the function defined by $f(x) = 3x^2 - x^3$. What is the absolute minimum value of f on the closed interval $[1, \frac{5}{2}]$?

$$f(1) = 3 - 1 = 2$$

$$f\left(\frac{5}{2}\right) = \frac{75}{4} - \frac{125}{8} = \frac{35}{8}$$



a rel. min
BUT not
on the
interval
so we
don't need
to find $f(0)$

- (A) 0
- (B) 2
- (C) $\frac{25}{8}$
- (D) 4

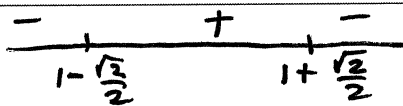
27

At what values of x does the graph of $y = x^2 e^{-2x}$ have a point of inflection?

NOTE: Generally the AP test does NOT have you use the QUADRATIC FORMULA!

Tough Algebra!

- (A) $x = -2$ and $x = 0$
- (B) $x = 0$ and $x = 1$
- (C) $x = -2 - \sqrt{2}$ and $x = -2 + \sqrt{2}$
- (D) $x = 1 - \frac{\sqrt{2}}{2}$ and $x = 1 + \frac{\sqrt{2}}{2}$



$$y' = x^2(-2e^{-2x}) + 2x \cdot e^{-2x} \Rightarrow y' = e^{-2x}(-2x^2 + 2x)$$

$$y'' = e^{-2x}(-4x + 2) + (-2x^2 + 2x) \cdot e^{-2x} \cdot (-2)$$

$$y'' = e^{-2x}(-4x + 2 - 2(-2x^2 + 2x))$$

$$y'' = e^{-2x}(-4x + 2 + 4x^2 - 4x)$$

$$y'' = e^{-2x}(4x^2 - 8x + 2)$$

$$y'' = 2e^{-2x}(2x^2 - 4x + 1)$$

$0 = 2e^{-2x}$
NO SOLUTION

or $0 = 2x^2 - 4x + 1$
needs QUADRATIC FORMULA

$$x = \frac{4 \pm \sqrt{16 - 4(2)(1)}}{2(2)}$$

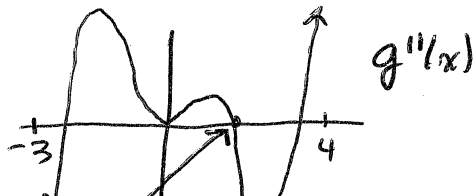
$$x = \frac{4 \pm \sqrt{8}}{4}$$

$$x = \frac{4 \pm 2\sqrt{2}}{4}$$

$$\frac{2 \pm \sqrt{2}}{2}$$

$$1 \pm \frac{\sqrt{2}}{2}$$

28) Graphing Calculator Needed

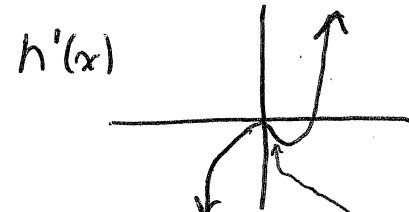


The second derivative of the function g is given by $g''(x) = x^5 - 2.2x^4 - 6.61x^3 + 8.602x^2$. At which values of x in the interval $-3 < x < 4$ does the graph of g have a point of inflection where the concavity of the graph changes from concave up to concave down?

when, f'' changes from positive to negative

- (A) $x = 1.1$ only
- (B) $x = -2.3$ and $x = 3.4$ only
- (C) $x = -2.3, x = 1.1,$ and $x = 3.4$ only
- (D) $x = -2.3, x = 0, x = 1.1,$ and $x = 3.4$

29) Graphing Calculator Needed



The first derivative of the function h is given by $h'(x) = x^5 - 3x^2 + x$. What are all intervals on which the graph of h is concave down? *when $h'(x)$ is DECREASING*

- (A) $(-\infty, 0)$ and $(0.338, 1.307)$
- (B) $(-\infty, 0.669)$
- (C) $(-\infty, 0.167)$ and $(1, \infty)$
- (D) $(0.167, 1)$

$$\frac{d^2y}{dx^2} = -2x - \left[x \frac{dy}{dx} + y \cdot 1 \right] + 2y \frac{dy}{dx}$$

$$= -2x - x \frac{dy}{dx} - y + 2y \frac{dy}{dx}$$

$$\frac{d^2y}{dx^2}(-1, 1) = -2(-1) - 0 - 1 + 0$$

$$= 2 - 1 = 1$$

30) Let f be a function such that $f(-1) = 1$. At each point (x, y) on the graph of f , the slope is given by

$$\frac{dy}{dx} = -x^2 - xy + y^2 - 1. \text{ Which of the following statements is true?}$$

$$\frac{dy}{dx}(-1, 1) = -1 - (-1) + 1 - 1 = 0$$

$$\frac{d^2y}{dx^2} = \text{POSITIVE VALUE}$$

- (A) f has a relative minimum at $x = -1$.
slope of zero on a cc up portion of the graph
- (B) f has a relative maximum at $x = -1$.
- (C) f has neither a relative minimum nor a relative maximum at $x = -1$.
- (D) There is insufficient information to determine whether f has a relative minimum, a relative maximum, or neither at $x = -1$.

at $(-1, 1)$
 so graph is cc up

31) Let f be a twice-differentiable function. Which of the following statements are individually sufficient to conclude that $x = 2$ is the location of the absolute maximum of f on the interval $[-5, 5]$?

~~I. $f'(2) = 0$ could be min, max, or plateau~~

II. $x = 2$ is the only critical point of f on the interval $[-5, 5]$, and $f''(2) < 0$.

III. $x = 2$ is the only critical point of f on the interval $[-5, 5]$, and $f(-5) < f(5) < f(2)$.

if it is the ONLY critical value on a cc down graph, that relative max must also be the absolute max

- (A) II only
- (B) III only
- (C) I and II only
- (D) II and III only

32)

x	0	1	2	3	4	5
$f'(x)$	-3	0	-1	5	0	-3
$f''(x)$	5.3	-2.0	1.7	-0.5	1.2	-5.1

Let f be a twice-differentiable function. Selected values of f' and f'' are shown in the table above. Which of the following statements are true?

NOTE: we can't assume other values

I. f has neither a relative minimum nor a relative maximum at $x = 1$.

II. f has a relative maximum at $x = 1$.

$f'(1) = 0$ $f''(1) < 0$ (so cc down)

III. f has a relative maximum at $x = 4$.

$f'(4) = 0$ $f''(4) > 0$ (so cc up) → a relative MIN!

MIN

(A) I only

(B) II only

(C) III only

(D) I and III only

33) Let f be the function defined by $f(x) = \frac{1}{3}x^3 - 3x^2 - 16x$. On which of the following intervals is the graph of f both decreasing and concave down?

$f'(x) = x^2 - 6x - 16$ $f''(x) = 2x - 6$
 $= (x-8)(x+2)$

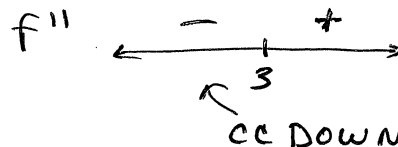
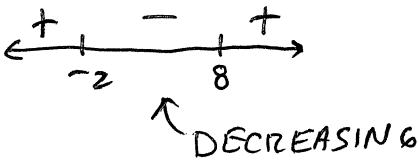
(A) $(-\infty, 3)$

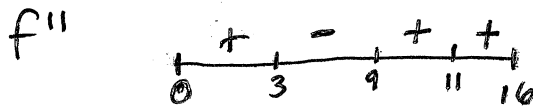
(B) $(-2, 3)$ only

(C) $(3, 8)$

(D) $(8, \infty)$

f'





34)

x	$0 < x < 3$	$x = 3$	$3 < x < 9$	$x = 9$	$9 < x < 11$	$x = 11$	$11 < x < 16$
$f'(x)$	Positive	Undefined	Negative	-3	Negative	0	Positive
$f''(x)$	Positive	Undefined	Negative	0	Positive	0	Positive

The function f is continuous on the interval $(0, 16)$, and f is twice differentiable except at $x = 3$, where the derivatives are undefined. Information about the first and second derivatives of f for values of x in the interval $(0, 16)$ is given in the table above. At what values of x in the interval $(0, 16)$ does the graph of f have a point of inflection?

(A) $x = 9$ only

(B) $x = 3$ and $x = 9$

(C) $x = 3$ and $x = 11$

(D) $x = 9$ and $x = 11$

35) Graphing Calculator Needed

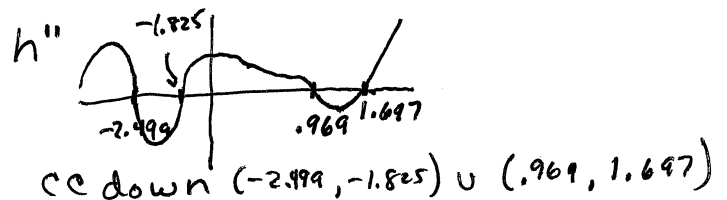
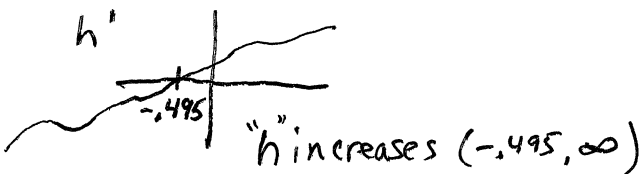
The first derivative of the function h is given by $h'(x) = \sin x + \cos(x^2) + x$, and the second derivative of h is given by $h''(x) = \cos x - 2x \sin(x^2) + 1$. On what open intervals contained in $-3 < x < 2$ is the graph of h both increasing and concave down?

(A) $(0.969, 1.697)$ only

(B) $(-2.499, -1.829)$ and $(0.969, 1.697)$

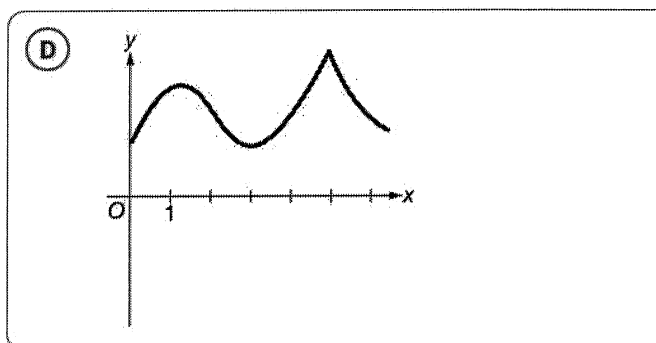
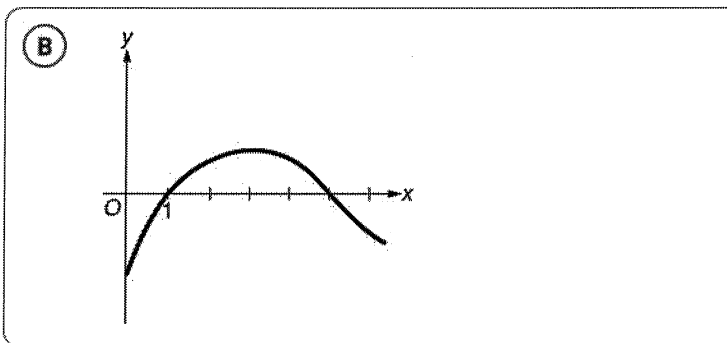
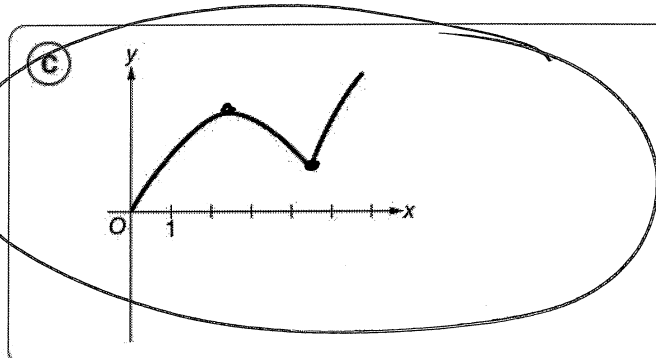
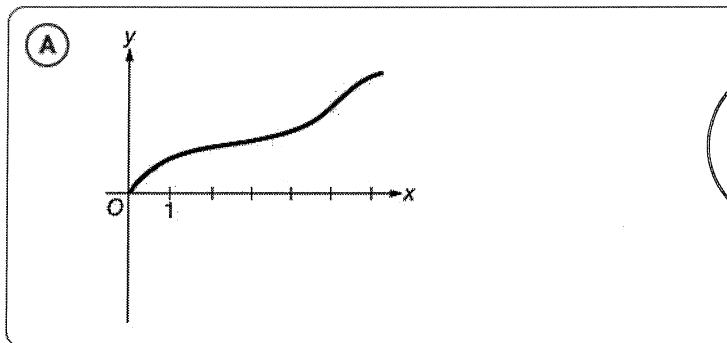
(C) $(-0.495, 2)$

(D) $(-1.311, -0.166)$

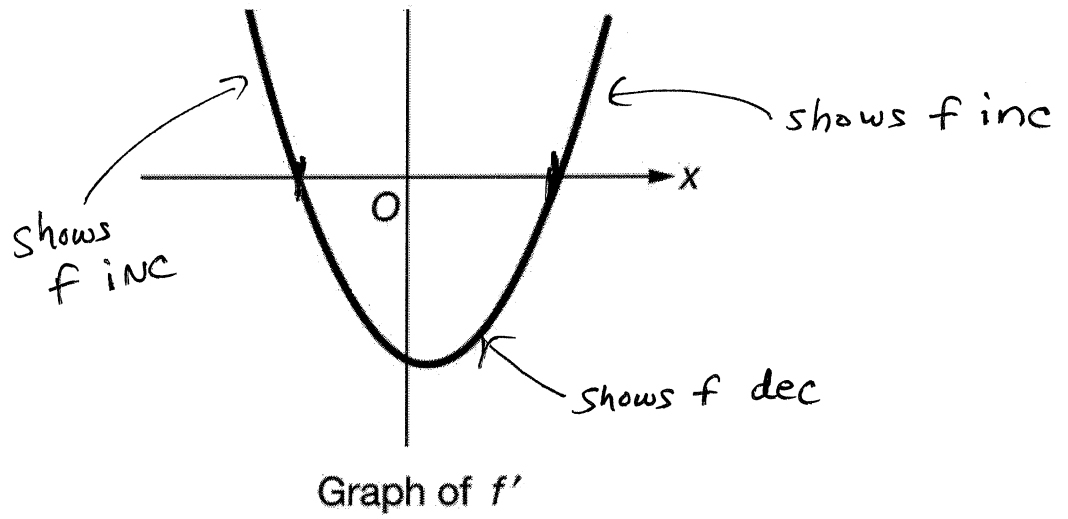


36) The function f is differentiable and increasing on the interval $0 \leq x \leq 6$, and the graph of f has exactly two points of inflection on this interval. Which of the following could be the graph of f' , the derivative of f ?

(two rel. min/max)



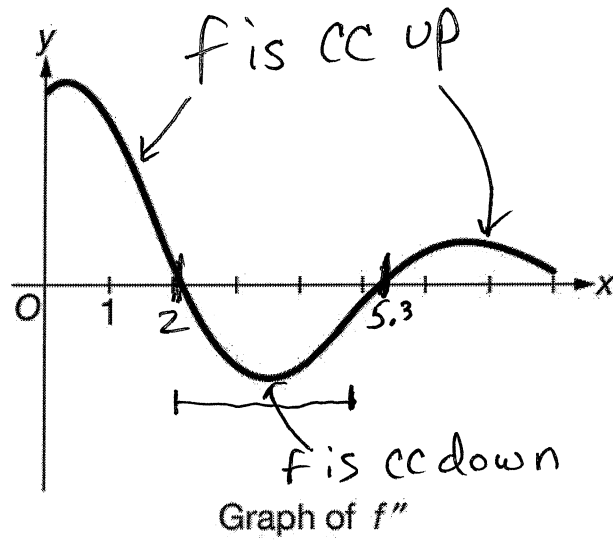
37)



The graph of f' , the derivative of the function f , is shown above. Which of the following could be the graph of f ?

<p>(A)</p>	<p>(C)</p>
<p>(B)</p>	<p>(D)</p>

38)



The graph of f'' , the second derivative of the function f , is shown above on the interval $0 \leq x \leq 8$. Which of the following could be the graph of f ?

(A)

(C)

(B)

(D)

1st deriv. $x^2 \frac{dy}{dx} + 2xy = 0 \quad \frac{dy}{dx} = \frac{-2xy}{x^2} = \frac{-2y}{x}$

2nd deriv. $\frac{x \cdot (-2 \frac{dy}{dx}) - (-2y) \cdot 1}{x^2} = \frac{d^2y}{dx^2} \quad \frac{d^2y}{dx^2} = \frac{-2x \cdot \frac{-2y}{x} + 2y}{x^2} = \frac{4y}{x^2}$

39) Let C be the curve defined by $x^2y = 4$. Which of the following statements is true of curve C at the point

(2,1)? $\frac{dy}{dx}(2,1) = \frac{-2(1)}{2} = -1$ $\frac{d^2y}{dx^2}(2,1) = \frac{4(1)}{2^2} = 1$
 $\frac{dy}{dx} < 0$ $\frac{d^2y}{dx^2} > 0$

(A) It has a relative minimum because $y' = 0$ and $y'' > 0$.

(B) It has a relative maximum because $y' = 0$ and $y'' < 0$.

(C) It is decreasing and concave up because $y' < 0$ and $y'' > 0$.

(D) It is decreasing and concave down because $y' < 0$ and $y'' < 0$.

40) Consider the curve defined by $\frac{x^2}{16} - \frac{y^2}{9} = 1$. It is known that $\frac{dy}{dx} = \frac{9x}{16y}$ and $\frac{d^2y}{dx^2} = -\frac{81}{16y^3}$. Which of the following statements is true about the curve in Quadrant IV?

$\leftarrow x$ is positive & y is negative

(A) The curve is concave up because $\frac{dy}{dx} > 0$.

(B) The curve is concave down because $\frac{dy}{dx} < 0$.

(C) The curve is concave up because $\frac{d^2y}{dx^2} > 0$.

(D) The curve is concave down because $\frac{d^2y}{dx^2} < 0$.

$\frac{dy}{dx}(+, -) < 0$ Decreasing

$\frac{d^2y}{dx^2}(+, -) > 0$ CC up